

type classes

So, what is the type of 42?

```
42 :: Num a => a
```

What does this mean?

Num is a type class.

Num a is a type class constraint.

Num a => a means some type a in the class Num.

And what is the Num class? All types in this class must implement addition, subtraction, multiplication, negation, absolute value, and other. See Haskell documentation for details.

type classes

Type classes offer a controlled approach to overloading.

There are a number of predefined type classes: Eq, Ord, Show, Read, Num, and more.

You can create instances of these classes.

You can also create your own classes and instantiate them.

(These are NOT like Python/Java classes. More like Java interfaces.)

type classes

The Eq type class is all types with equality defined.

Types in this class provide == and /=.

```
member _ [] = False
member y (x : xs) = x == y || member y xs
```

```
prompt> :type member
```

```
member :: (Eq t) => t -> [t] -> Bool
```

(Eq t) is a type class constraint.

All the base types (Int, Bool, etc.) are members of Eq.

Let's look more closely at what type classes are.

type classes

A simple way to create a member of Eq:

```
data Btree a = Empty | Node (Btree a) a (Btree a)
               deriving Eq
```

```
prompt> (Node Empty 4 Empty) == (Node Empty 5 Empty)
False
```

```
prompt> (Node Empty 4 Empty) /= (Node Empty 5 Empty)
True
```

```
prompt> (Node Empty 4 Empty) == (Node Empty 4 Empty)
True
```

type classes

We may wish to provide a non-derived equality method.

```
data First = Pair Int Int
```

```
instance Eq First where
```

```
    (Pair x _) == (Pair y _) = (x == y)
```

```
prompt> (Pair 1 3) == (Pair 2 3)
```

```
False
```

```
prompt> (Pair 1 3) == (Pair 1 4)
```

```
True
```

type classes

More general:

```
data First a = Pair a a
```

```
instance Eq a => Eq (First a) where  
    (Pair x _) == (Pair y _) = (x == y)
```

```
prompt> (Pair [1, 2, 3] [1]) == (Pair [1, 2, 3] [3])
```

```
True
```

```
prompt> (Pair [1] [2]) == (Pair [2] [2])
```

```
False
```

type classes

Providing a **default definition** of a function in the type class definition:

```
class Eq a where
  (==), (/=) :: a -> a -> Bool
  x /= y = not (x == y)
  x == y = not (x /= y)
```

Either of these default definitions may be overridden.

```
prompt> (Pair [1, 2, 3] [1]) /= (Pair [1, 2, 3] [3])
False
prompt> (Pair [1] [2]) /= (Pair [2] [2])
True
```

type classes

`Ord` inherits from `Eq` and specifies the four comparison operators `<`, `<=`, `>`, `>=`. It gives default definitions for `min` and `max` in terms of these.

There is also a three-way `compare` function which returns `LT`, `EQ`, and `GT`.

Most basic datatypes are instances of `Ord`, and user-defined datatypes can derive `Ord` (lexicographic ordering).

type classes

Show specifies the method `show :: a -> String`.

Read specifies the method `read :: String -> a` and can be used for parsing.

Num inherits from Eq, and specifies `+`, `-`, `*`, `negate`, `abs`, and `signum`.

Division is handled by `Integral` and `Fractional`, which inherit from Num.

Use `:info <typeclass>` to see the instances of a typeclass.

type classes

Defining our own type class:

```
class YesNo a where
  yesno :: a -> Bool
```

and some instances:

```
instance YesNo Integer where
  yesno 0 = False
  yesno _ = True
```

```
instance YesNo [a] where
  yesno [] = False
  yesno _ = True
```

type classes

```
instance YesNo Bool where
    yesno x = x

instance YesNo (BTree a) where
    yesno Empty = False
    yesno _ = True
```

Then

```
prompt> yesno []
False
prompt> yesno ""
False
prompt> yesno [1, 2, 3]
True
prompt> yesno "abc"
True
```

type classes

cont.

```
prompt> yesno Empty
```

```
False
```

```
prompt> yesno (Node "a" Empty Empty)
```

```
True
```

```
prompt> yesno True
```

```
True
```

```
prompt> yesno (1 == 0)
```

```
False
```

```
prompt> yesno 0
```

```
False
```

```
prompt> yesno 42
```

```
True
```

type classes

cont.

```
prompt> :t yesno
```

```
yesno :: (YesNo a) => a -> Bool
```

```
prompt> :info YesNo
```

```
class YesNo a where yesno :: a -> Bool
```

```
  -- Defined at /...path.../filename.hs:140:6-10
```

```
instance YesNo Integer
```

```
  -- Defined at /...path.../filename.hs:(143,0)-(145,17)
```

```
instance YesNo [a]
```

```
  -- Defined at /...path.../filename.hs:(147,0)-(149,17)
```

```
instance YesNo Bool
```

```
  -- Defined at /...path.../filename.hs:(151,0)-(152,19)
```

```
instance YesNo (BTree a)
```

```
  -- Defined at /...path.../filename.hs:(154,0)-(156,17)
```